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Review article

The reign of the P value is over: what alternative analyses could we employ to fill the power vacuum?

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Keywords: AIC, Bayesian, confidence intervals, effect size, statistical analysis

Abstract

The P value has long been the figurehead of statistical analysis in biology, but its position is under threat. P is now widely recognised as providing quite limited information about our data, and as being easily misinterpreted. Many biologists are aware of P’s frailties, but less clear about how they might change the way they analyse their data in response. This article highlights and summarises four broad statistical approaches that augment or replace the P value, and that are relatively straightforward to apply. First, you can augment your P value with information about how confident you are in it, how likely it is that you will get a similar P value in a replicate study, or the probability that a statistically significant finding is in fact a false positive. Second, you can enhance the information provided by frequentist statistics with a focus on effect sizes and a quantified confidence that those effect sizes are accurate. Third, you can augment or substitute P values with the Bayes factor to inform on the relative levels of evidence for the null and the alternative hypotheses; this approach is particularly appropriate for studies where you wish to keep collecting data until clear evidence for or against your hypothesis has accrued. Finally, specifically where you are using multiple variables to predict an outcome through model building, Akaike information criteria can take the place of the P value, providing quantified information on what model is best. I hope this quick-and-easy guide to some simple yet powerful statistical options will support biologists in adopting new approaches where they feel that the P value alone is not doing their data justice.

37 **Main text**

38 The reified position of the P value in statistical analyses was unchallenged for decades despite
39 criticism from statisticians and other scientists [e.g. 1, 2-4]. In recent years, however, this unrest has
40 intensified, with a plethora of new papers either driving home previous arguments against P or
41 raising additional critiques [e.g. 5, 6-11]. Catalysed by the part that the P value has played in
42 science's reproducibility crisis, this criticism has brought us to the brink of an uprising against P's
43 reign.

44 Consequently, an analysis power vacuum is forming, with a range of alternative approaches vying to
45 fill the space. Commentaries that criticise the P value often suggest alternate paradigms of statistical
46 analysis, and now a number of options have taken seed in the field of biology. New statistical
47 methods typically involve concepts that are counter-intuitive to our P-based training; they represent
48 radically different ways of interrogating data that involve disparate approaches to generating
49 evidence, different software packages, and a host of new assumptions to understand and justify. The
50 steep learning curves for new methods could stifle the progress made in biology in moving away
51 from P-centred statistical analyses.

52 To provide clarity and confidence for biologists seeking to expand and diversify their analytical
53 approaches beyond a focus on P, this article summarises some tractable alternatives to P value
54 centrality. But first, here is a brief overview about the limits of the P value and why, on its own, it is
55 rarely sufficient to interpret our hard-earned data. Along with many other august statisticians, Jacob
56 Cohen and John Tukey have written cogently about their concerns with the fundamental concept of
57 null hypothesis significance testing. Because the P value is predicated on the null hypothesis being
58 true, it does not give us any information about the alternative hypothesis – the hypothesis we are
59 usually most interested in. Compounding this problem, if our P value is high and so does not reject
60 the null hypothesis this cannot be interpreted as the null being true; rather, we are left with an
61 'open verdict' [2]. Moreover, with a big enough sample size inevitably the null hypothesis will be
62 rejected; perversely, a statistical result is as informative about our sample as it is about our
63 hypothesis [12, 13].

64 Recently, further concerns have been documented about P, linking the P value to problems with
65 experimental replication [5]. Cumming [7] and Halsey et al. [6] demonstrated that P is 'fickle' in that
66 it can vary greatly between replicates even when statistical power is high, and argued that this
67 makes interpretation of the P value untenable unless P is extremely small. Colquhoun [8, 14] has
68 argued that significant P values at just below 0.05 are extremely weak evidence against the null
69 hypothesis because there is a 1 in 3 chance that the significant result is a false positive (aka type 1
70 error). Interpreting P dichotomously as 'significant' or 'not significant' is particularly egregious for
71 many reasons, but most pertinent here is that this approach encourages failed experiment
72 replication. Studies are often designed to have 80% statistical power, meaning that there is an 80%
73 chance that an effect in the data will be detected. As Wasserstein & Lazar [9] explain, the probability
74 of two identical studies statistically powered to 80% both returning $P \leq 0.05$ is at best $80\% * 80\% =$
75 64% , while the probability of one of these studies returning $P \leq 0.05$ and the other not is $2 * 80\% *$
76 $20\% = 32\%$. Together, these papers and calculations demonstrate that the P value is typically highly
77 imprecise about the amount of evidence against the null hypothesis, and thus P should be
78 considered as providing only loose, first pass evidence about the phenomenon being studied [6, 15,
79 16].

80 With the broadening realisation among biologists that P values provide only tentative evidence
81 about our data – and, indeed, that exactly what this evidence tells us is easy to misinterpret – it is

82 important that we equip ourselves with a broad understanding of what statistical options are
83 available that can clarify, or even supplant, P. While it will be hard to extricate ourselves from our
84 indoctrinated approach to interpreting every statistical analysis through the prism of significance or
85 non-significance, we can be motivated by the knowledge that there really are other ways, and
86 indeed more intuitive ways, to investigate our data. Below, I provide a quick-and-easy guide to some
87 simple yet powerful statistical options currently available to biologists conducting standard study
88 designs. Each distinct statistical approach interrogates the data through a different lens, i.e. by
89 asking a fundamentally different scientific question; this is reflected in the subsection headings that
90 follow. We shall start with the option least disruptive to the P value paradigm – augmenting P with
91 information about its variability.

92 *P value: How much evidence is there against the null hypothesis?*

93 P provides unintuitive information about your data. However, it can perhaps best be interpreted as
94 characterising the evidence in the data against the null hypothesis [10, 17]. And despite its
95 limitations, the P value has attractive qualities. It is a single number from which an objective
96 interpretation about data can be made. Moreover, that interpretation is context independent; P
97 values can be compared across different types of studies and statistical tests [18]. Huber [19] argues
98 that focussing on the P value is a suitable first step for screening of multiple hypotheses, as occurs in
99 ‘high throughput biology’ such as gene expression analysis and genome-wide association studies.

100 However, P is let down by the considerable variability it exhibits between study samples; variability
101 disguised by the reporting of P as a single value to several decimal places. Arguably, then, if you
102 want to continue calculating P as part of your analyses of individual tests, you ought to provide some
103 additional information about this variability, to inform the reader about the uncertainty of this
104 statistic. One way to achieve this is to provide a value that is somewhat akin to the confidence
105 interval around an effect size, that characterises the uncertainty of your study P value and is termed
106 the P value prediction interval [7]. Another option is to calculate the prediction interval that
107 characterises the uncertainty of the P value of a future replicate study. Lazzeroni et al. (2016)
108 provide a simple online calculator for both (<https://www.nature.com/articles/nmeth.3741#s1>).
109 Based on this calculator, if the P value from your experiment is, for example, 0.01, it will have a 95%
110 prediction interval of 5.7×10^{-6} to 0.54. Clearly, this would provide us with little confidence that P is
111 replicable under this experimental scenario. A P value of 0.0001 has a 95% prediction interval of 0 to
112 0.05. In this second scenario, the 95% prediction interval of a future replicate study is 0 to 0.26.
113 Vsevolozhskaya et al. [20] argue that the prediction interval around P calculated by this method
114 returns underestimates of both the lower and upper bounds. Nonetheless, the width of the
115 prediction interval, however calculated, will be surprisingly large to those of us accustomed to
116 seeing the P value as a naked single value reported to great precision.

117 If you have calculated the planned power of your study, and are prepared to quantify the level of
118 belief you had before conducting the experiment that the null hypothesis is true, you can augment P
119 with the estimated likelihood that if you get a significant P value it is falsely rejecting the null
120 hypothesis. This is termed the estimated false positive (discovery) risk, and can be easily estimated
121 from a simple Bayesian framework (see later) [21, 22]:

122 Estimated false positive risk = $P \cdot \pi_0 / (P \cdot \pi_0 + (1 - \beta)(1 - \pi_0))$,

123 where P = the P value of your study, π_0 = the probability that the null hypothesis is true based on
124 prior evidence, $(1 - \beta)$ = study power.

125 For example, if you have powered your study to 80% and before you conduct your study you think
126 there is a 30% possibility your perturbation will have an effect (thus $\pi_0 = 0.7$), and then having
127 conducted the study your analysis returns $P = 0.05$, the estimated false positive risk is 13%. That is,
128 many replicates of this experiment would indicate a statistically significant effect of the perturbation
129 and be wrong in doing so about 13% of the time. Bear in mind, however, that given the
130 aforementioned fickleness of P , this estimate of false positive risk could be equally capricious. This
131 concern can be circumvented for high throughput studies, replacing P in the equation above for α
132 (the significance threshold of the statistical test), and estimating π_0 from observed P values [21, 22].

133 For those not conducting high throughput studies and who do not like the idea of quantifying their *a*
134 *priori* expectations about the veracity of their experimental perturbation, the calculations can be
135 flipped such that your P value is accompanied by a calculation of the prior expectation that would be
136 needed to produce a specified risk (e.g. 5%) of a significant P value being a false positive [8; and he
137 provides an easy-to-use web calculator for this purpose: <http://fpr-calc.ucl.ac.uk/>]. If, for example,
138 your P value is 0.03 for a study powered to about 70%, to limit the risk of a false positive to 5% your
139 prior expectation that the perturbation will have an effect would need to be 77% [based on the ‘P-
140 equals’ case; 8].

141 *Effect size and confidence interval: How much and how accurate?*

142 A statistically significant result tells us relatively little about the phenomenon we are studying - only
143 that the null hypothesis of no ‘effect’ in our data [which we already knew wasn’t true to some level
144 of precision; 13] has been rejected [23]. Instead of the P value scientific question ‘is there or isn’t
145 there an effect?’, considerably more information is garnered by asking ‘how strong is the effect in
146 our sample?’ coupled with the question ‘how accurate is that value as an estimate of how strong the
147 population effect is?’.

148 The most straightforward way to analyse your data in order to answer these two questions is to
149 calculate the effect size in the sample along with the 95% confidence intervals around that estimate
150 [6, 7, 24-27]. Fortunately, the effect size is often easy to calculate or extract from statistical outputs,
151 since it is typically the mean difference between two groups or the strength of the correlation
152 between two variables. And while the definition of a confidence interval is complex, Cumming and
153 Calin-Jageman [28] compellingly argue that it is reasonable to interpret a confidence interval as an
154 indication of the accuracy of the effect size estimate; it is the likely error estimation.

155 The calculations of confidence intervals and P values share the same mathematical framework [29,
156 30], but this does not detract from the fact that focussing interpretation of data on effect sizes and
157 their confidence intervals is a fundamentally different approach to that of focussing interpretation
158 on whether or not to reject the null hypothesis [11]. These two procedures ask very different
159 questions about the data and elicit distinct answers [31]. For example, a study on the effects of two
160 different ambient temperatures on paramecium size returning an effect size of 20 μm and a P value
161 of 0.1, if centred on P value interpretation would conclude ‘no effect’ of temperature, despite the
162 best supported effect size being 20, not 0. An interpretation based on effect size and confidence
163 intervals could, for example, state: ‘Our results suggest that paramecium kept at the lower
164 temperature will be on average 20 μm larger in size, however a difference in size ranging between -4
165 and 50 μm is also reasonably likely’. As Amrhein et al. (2019) point out, the latter approach
166 acknowledges the uncertainty in the estimated effect size while also ensuring that you do not make
167 a false claim either of no effect if $P > 0.05$, or an overly confident claim. And if all the values within
168 the confidence interval are biologically unimportant, then a statement that your results indicate no

169 important effect can also be made. (This is an example of where focussing on effect size and
170 uncertainty also allows clear yes/no interpretations if desired; see also [32]).

171 The approach of focussing on effect size estimation is usually accompanied by an emphasis on
172 visualisation of the data to support their evaluation, the graphics showing the raw data and side
173 panels helping to illustrate the estimated effect size (e.g. Supplementary Figure 1). Such plots, while
174 intuitive, are not typically available in statistical packages and not easy to code in programming
175 languages. However, Ho and colleagues [33] have recently developed 'Data Analysis with Bootstrap-
176 coupled ESTimation' (DABEST), available in versions for Matlab, Python and R, and also as a webpage
177 estimationstatistics.com. All versions have user-friendly, rote instructions to produce graphs that
178 allow full exploration of your data.

179 Scientific research seeks to home in on 'answers', and estimated effect sizes and their confidence
180 intervals are central to this goal. In biology at least, homing in on an answer almost inevitably
181 requires multiple studies, which then need to be analysed together, through meta-analysis. Effect
182 sizes and confidence intervals are the vital information for this process [e.g. 34], providing another
183 good argument for their thorough reporting in papers. Typically, the confidence intervals around an
184 effect size calculated from a meta-analysis are much smaller than those of the individual studies
185 [35], thus giving a much clearer picture about the true, population-level effect size (Figure 1).
186 However, meta-analyses can be deeply compromised by the 'file drawer phenomenon', where non-
187 significant results are not published [36], either because researchers do not submit them, or journals
188 will not accept them [37]. Fortunately, attitudes of science funders, publishers and researchers are
189 starting to change about the value and importance of reporting non-significant results; this
190 momentum needs to continue.

191 *Bayes factor: What is the evidence for one hypothesis compared to another?*

192 In contrast to the P value providing only information about the likelihood that the null hypothesis is
193 true, the Bayes factor directly addresses both the null and the alternative hypotheses. The Bayes
194 factor quantifies the relative evidence in the data you have collected about whether those data are
195 better predicted by the null hypothesis or the alternative hypothesis (an effect of stated magnitude).
196 For example, a Bayes factor of 5 indicates that the strength of evidence is five times greater for the
197 alternative hypothesis than the null hypothesis; a Bayes factor of 1/5 indicates the reverse.

198 The Bayes factor is a simple and intuitive way of undertaking the Bayesian version of null hypothesis
199 significance testing. Only recently have Bayes factors been made tractable for the practicing
200 biologist, and these are now easily calculable for a range of standard study designs. The Bayes
201 factors for many designs can be run on web-based calculators (e.g.
202 <http://pcl.missouri.edu/bayesfactor>) and are also available as a new package for R called
203 BayesFactor() [38].

204 A controversy of the Bayesian approach is the need for you to specify your strength of belief in the
205 effect being studied before the experiment takes place (the prior distribution of the alternative
206 hypothesis) [39]. Thus, your somewhat subjective choice of 'prior' influences the outcome of the
207 analysis. Schonbrodt et al. (2017) argue that this criticism of Bayesian statistics is often exaggerated
208 because the influence of the prior is limited when a reasonable prior distribution is used. You can
209 assess the influence of the prior with a simple sensitivity analysis whereby the analysis is run using a
210 bounded range of realistic prior probabilities [40]. There is also a default prior that you can use in
211 the common situation that you have little pre-study evidence for the expected effect size.

212 Nonetheless, undertaking Bayesian analyses is more involved than null hypothesis significance
213 testing, and specifying the prior undoubtedly adds some degree of subjectivity. Fortunately, there is
214 a single, simple formula that you can apply to convert a P value to a form of the Bayes factor without
215 any other information. This simplified Bayes factor, termed the upper bound, states the most likely it
216 is that the alternative hypothesis (of an effect) is true rather than the null hypothesis over any
217 reasonable prior distribution [comment by Benjamin and Berger annexed to 9, 41]:

218 Bayes factor upper bound $\leq -1/(e \cdot P \cdot \ln(P))$

219 For example, if your data generate a P value of 0.07 (sometimes termed a 'trend'), the Bayes factor
220 upper bound is 1.98 and you can conclude that the alternative hypothesis is at most twice as likely as
221 the null hypothesis. A P value of 0.01 indicates the alternative hypothesis is at most 8 times as likely
222 as the null. Benjamin and Berger argue that this approach is an easily-interpretable alternative to P,
223 which should satisfy both practitioners of Bayesian statistics and practitioners of null hypothesis
224 significance testing [comment by Benjamin and Berger annexed to 9].

225 Schönbrodt et al. [42] make the case that the Bayes factor can be used to inform when a study has
226 secured a sufficient sample size and can be halted. Effective stopping rules in research can be
227 invaluable for controlling time and financial costs while increasing study replicability, and are
228 ethically important for certain animal studies or intrusive human studies; the use of subjects should
229 be minimised while ensuring the experiments are robust and reproducible
230 [<https://www.nc3rs.org.uk/the-3rs>; 43]. Arguably, stopping rules should be used a lot more than
231 they presently are, and can be a far more effective method for targeting a suitable sample size than
232 power analysis. A big mistake often made, however, is to implement the P value in the stopping rule;
233 the study is stopped when the data thus far collected return a statistically significant P value. The
234 underlying assumption is that increasing the sample size further would probably decrease P further.
235 A simple model demonstrates this thinking to be spurious and thus that it drives very bad practice
236 (Figure 2). For those of us basing our study on the P value, it is far preferable to continue a study
237 until a pre-determined sample size is reached that has been decided by *a priori* power analysis [44].
238 However, this approach is greatly influenced by the associated *a priori* effect size estimate we have
239 provided and there can be a strong temptation to increase sample size beyond the pre-determined
240 number; in their longing for a statistically significant result, the P values of 0.06 and 0.07 are a siren
241 call luring researchers into recording more data points [45].

242 The Bayes factor is much more appropriate here. It provides evidence for the null, and with a large
243 enough sample the Bayes Factor will converge on 0 (the null is true) or infinity (the alternative is
244 true). If the Bayes Factor of your data reaches 10 or 1/10, this almost certainly represents the true
245 situation and your study can stop. Alternatively, if your study must be stopped for logistical reasons
246 then the final Bayes Factor can still be interpreted, for example a Bayes factor of 1/7 would indicate
247 moderate evidence for the null hypothesis. Moreover, you are entitled to continue sampling if you
248 feel the data are not conclusive enough; if the results are unclear, collect more data. All such
249 decisions do not affect interpretation of the Bayes Factor [42]. A final big motivation for employing
250 the Bayes factor over the P value in stopping procedures is that in the long run, the former uses a
251 smaller sample while at the same time generating less interpretation errors. A general consensus has
252 not yet been reached about the most suitable priors for each situation, and tractable Bayes factor
253 procedures have thus far only been produced for some experimental designs, but do not let this put
254 you off. Instead of the Bayes factor, the Bayes factor upper bound, as described above, can be used.

255 *Akaike Information Criterion: What is the best understanding of the phenomenon being studied?*

256 If your study involves measuring an outcome variable and multiple potential explanatory variables,
257 then you have many possible models you could build to explain the variance in your data. Stepwise
258 procedures of model building often focus on P values, by holding onto only those explanatory
259 variables associated with a low P. Aside from the general concerns about P, specific criticisms of P
260 value-based model building include the inflated risk of type 1 errors [46, 47]. An alternative
261 approach to model assessment is the Akaike information criterion (AIC), which can be easily
262 calculated in statistical software packages, and in R using AIC() [48]. The AIC provides you with an
263 estimate of how close your model is to representing full reality [49], or in other words its predictive
264 accuracy [50]. Couched within the principle of simplicity and parsimony, a fundamental aspect of the
265 AIC is that it trades off the goodness of fit of a model against that model's complexity to ensure
266 against over-fitting [51].

267 Let's imagine you have generated three models, returning AICs of 443 (model 1), 445 (model 2) and
268 448 (model 3). Your preferred model in terms of relative quality will be the one that returns the
269 minimum AIC. But you should not necessarily discard the other models. With the AIC calculated for
270 multiple models, you can easily compute the relative likelihood that each of those models is the best
271 of all presented models given your data, i.e. the relative evidence for each of them. For example, the
272 preferred model will always have a relative evidence of 1, and in the current example the second
273 best model, model 2, has relative evidence 0.37, and model 3 has 0.08. Finally, you can then
274 compute an evidence ratio between any pair of models; following the above example, the evidence
275 for model 1 over model 2 is $1/0.37 = 4.6$, i.e. the evidence for model 1 is 2.7-times as strong. In this
276 scenario, although model 1 has the absolute lowest AIC, the evidence that model 1 rather than
277 model 2 is the best from those generated is not strong, and with some explanatory variables present
278 in only one of the models, the most suitable response could be to make your inferences based on
279 both models [49]. The AIC approach encourages you to think hard about alternative models and thus
280 hypotheses, in contrast to P value interpretation that encourages rejecting the null when P is small,
281 and supporting the alternative hypothesis by default [52]. More broadly, the AIC paradigm involves
282 dropping hypotheses judged implausible, refining remaining hypotheses and adding new hypotheses
283 – a scientific strategy that Burnham et al. [49] argue promotes fast and deep learning about the
284 phenomenon being studied.

285 Although the AIC is mathematically related to the P value [they are different transformations of the
286 likelihood ratio; 30], the former is far more flexible in the models it can compare. The AIC is a strong
287 option for choosing between multiple models that you have generated to explain your data, i.e. to
288 choose what model represents your best understanding of the phenomenon you have measured,
289 particularly when the observed data are complex and poorly understood and you do not expect your
290 models to have particularly strong predictive power [53]. A word of caution is important here,
291 however - it is easy to misuse AIC and you should be careful to ensure the models analysed are linear
292 and have normally distributed residuals.

293 A key limitation of the AIC is that it provides a relative, not absolute, test of model quality. It is easy
294 to fall into the trap of assuming that the best model is also a good model for your data; this may be
295 the case, or instead the best model may have only half an eye on the variance in your data while all
296 other models are blind to it. To quantify the absolute quality of your best model(s) requires
297 calculation of the effect size, as discussed earlier (in the case of models, typically R^2 is suitable).

298 **Conclusions**

299 Good science generates robust data ripe for interpretation. There are several broad approaches to
300 the statistical analysis of data, each interrogating the collected variables through a distinct line of

301 questioning. Popper [54] argued that science is defined by the falsifying of its theories. Taking this
302 approach to science, P values might be the rightful centrepiece of your statistical analysis since they
303 provide evidence against the null hypothesis [10, 17]. Building on this paradigm, you can easily
304 enhance interpretation of the P value by augmenting P with a prediction interval and/or an estimate
305 of the false positive risk - information about P's reliability. A counter argument, however, is that
306 because the P value does not test the null hypothesis nor the alternative hypothesis you can never
307 use it to actually falsify a theory [55]. Converting the P value into a Bayes factor attends to this
308 concern, providing relative evidence for one hypothesis or the other. But many have argued that
309 hypothesis testing by any approach is superseded by focussing on the effect in the data – specifically
310 both its magnitude and accuracy – because your best estimate of the magnitude of the phenomenon
311 you are studying is ultimately what you want to know. And if you conduct multi-variate analysis,
312 particularly when the phenomenon under study is poorly understood, you can be well served by the
313 AIC, which encourages consideration of multiple hypotheses and their gradual refinement.

314

315 It is important to impress that these manifold approaches are not all mutually exclusive, for example
316 many would argue that effect size estimates are an essential component of most analyses. Indeed,
317 Goodman et al. [56] go so far as to recommend the use of a hybrid for decision making that requires
318 a low P value coupled with an effect size above an *a priori* determined minimum to be
319 relevant/important in order to reject the null hypothesis. P values can also be presented alongside
320 Bayes factors for each statistical test conducted ('a B for every P'). Continuing to present P values as
321 part of your statistical output while diluting their interpretive power by including other statistical
322 approaches is possibly the best way to nudge reviewers and editors towards accepting, even
323 encouraging, the application of alternate inferential paradigms and without jeopardising your
324 submission [and see Box 2 in 43]. Whatever your chosen statistical approach, it is important that this
325 has been determined before data collection. Arming oneself with more statistical options could risk
326 the temptation of trying different approaches until an exciting result is achieved; this must be
327 resisted.

328

329 Regardless of the statistical paradigm you employ to investigate patterns in your data, many have
330 recommended that the outputs from statistical tests should always be considered as secondary
331 interrogations. Primarily, the argument goes, you should prioritise interpretation of graphical plots
332 of your data, at least where this is possible, and treat statistical analyses as supporting or
333 confirmatory information to what can be visualised [26, 57-59]. A plot that does not appear to
334 support the findings of your statistical analysis should not be automatically explained away as a
335 demonstration that your analysis has uncovered patterns deeper than can be visualised.

336

337 Finally, while I hope that this review might help readers feel a little more aware of, and confident
338 about, some of the additional and alternative statistical options to the P value, it is worth reminding
339 ourselves of Sir Ronald Fisher's pertinent words: 'To call in a statistician after the experiment is done
340 may be no more than asking him to perform a post-mortem examination: he may be able to say what
341 the experiment died of.' Without a good data set, none of the statistical tools mentioned here will
342 be effective. Moreover, even a good data set represents just a single study, and it must not be
343 forgotten that a single study provides limited information. Ultimately, replication is key to refining,
344 and having confidence in, our understanding of the biological world.

345

346 **Acknowledgements**

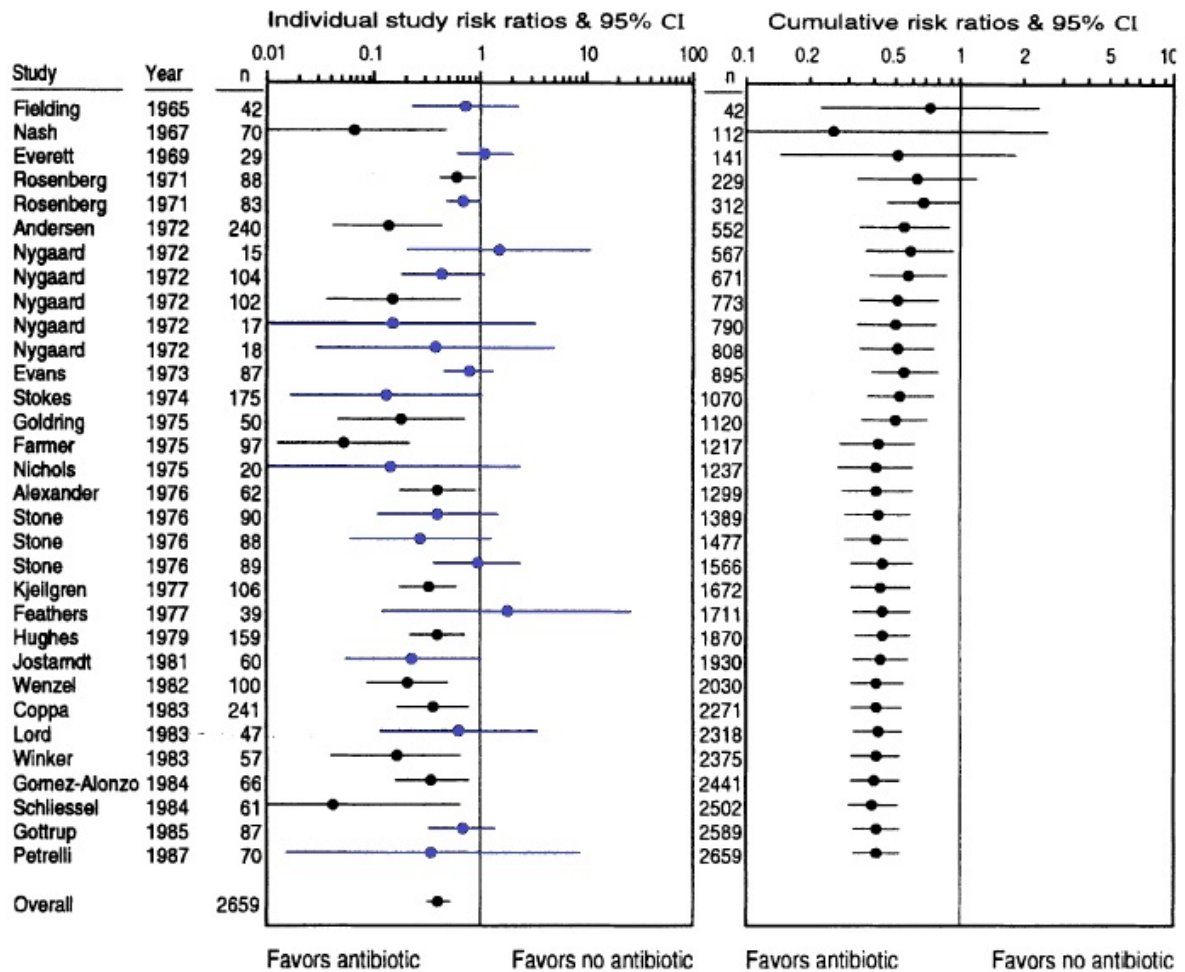
347 I appreciate the feedback that I received on drafts of this article from Michael Pedersen, Drs Louise
348 Soanes and Mircea Iliescu, and Professor Stuart Semple.

349
350 Data accessibility
351 All data were generated by R code, made available.

352 Funding
353 This study was not supported by funding.

354 Competing interests
355 I have no competing interests.

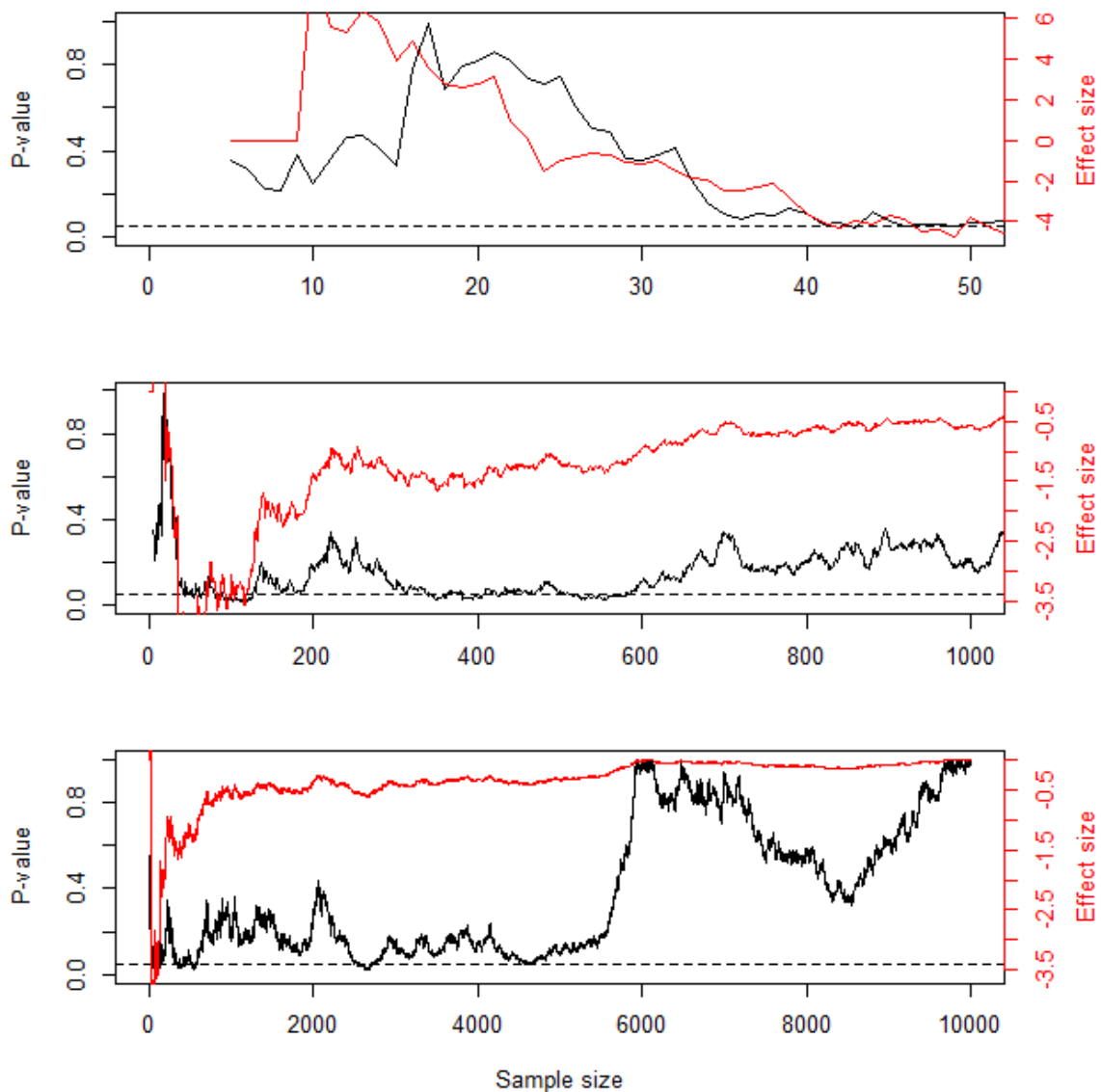
356 Ethical statement
357 Consent was not required for this review.
358



359

360 Figure 1. Standard and cumulative meta-analyses of studies investigating antibiotic prophylaxis for
 361 colon infection compared to the control of no treatment. In the left panel, the effect size and 95%
 362 confidence interval are shown for each study, which are displayed chronologically. Risk ratios (effect
 363 size) less than 1 favour a prophylactic; greater than 1 favours no treatment. n represents study
 364 sample size. The pooled result from all studies is shown at the bottom. Note that the studies where
 365 the confidence interval intersects 1 (coloured blue) would be interpreted as statistically non-
 366 significant (no efficacy of the prophylaxis); otherwise (black) as statistically significant (the
 367 prophylaxis is worth administering). Interpretation of all these studies based on the P value alone
 368 would not provide any clarification about the value of an antibiotic prophylaxis with treatment of
 369 colon infection, with around half the studies reporting statistical significance. The right panel
 370 represents a cumulative meta-analysis of the same studies (n represents cumulative sample size).
 371 This shows that some degree of efficacy of antibiotic prophylaxis for treatment in colon infection
 372 could have been identified as early as 1972, and well before the final study, the efficacy effect size
 373 was fairly clear. Figure (adapted) and some caption text taken from Ioannidis and Lau [60].

374



375

376 Figure 2. A demonstration of variability in the P value as data from a study are collected and
 377 analysed after each new addition to the sample. This can result in a study being stopped under the
 378 mistaken belief that as soon as a significant P value is obtained this reflects a real effect.

379 A computer simulates samples drawn at random from two identical, randomly distributed
 380 populations (standard deviation = 10), thus the null hypothesis is true. A Student's t test is
 381 conducted after five samples are drawn from the two populations. Subsequently, each time one
 382 further sample is taken for each population the t test is re-run. The evolution of the P value as
 383 sample size increases is presented in the three panels (black line), the upper panel showing the first
 384 50 samples, the middle the first 1000, and the lower panel showing up to 10 000 samples being
 385 drawn. The P value varies considerably; another demonstration of its 'fickleness' [6]. In each panel,
 386 the red line represents the effect size (mean difference between the samples). Although the P value
 387 should typically be high under these circumstances, reflecting a lack of evidence against the null,
 388 when the sample size is small it can easily decrease temporarily to below 0.05 (denoted by the
 389 dashed line) suggesting the populations from which the samples are drawn are different. If the
 390 sampling is stopped when this happens, P will be unrepresentative of reality and return a false

391 positive. (Note that in this simulation, P does not tend towards 0 as the sample size becomes very
392 large because as sample size increases the effect size tends towards 0 and thus statistical power
393 does not systematically increase [observed power is inversely related to P; 61]).

394 **References**

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